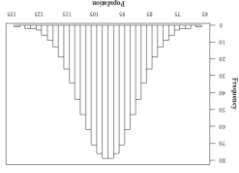


What is Normal, Anyway?

Basic Stat Vocabulary

Define the following terms, in your own words:

- Population
All members of a defined group.
- Sample
A subset of the population.
- Random Sample
A subset of the population where members must have:
 - An equal opportunity to be selected and*
 - The same characteristics of the population.*



in statistics!

The **normal distribution** is suitable for many naturally occurring variables and one of the most important distributions

Name: _____

- Mean (μ)
The arithmetic average; sum of the data values divided by the total number of data values.
- Variance (σ^2)
The arithmetic mean of the squared differences between each data value and the mean; Combines all of the values in a data set to produce a measure of spread.
- Standard Deviation (σ)
The square root of variance; the measure of spread of a distribution with the same units as the data.

Example

The lengths of adult Loggerhead sea turtle shells follow a normal distribution. It is known that 20% of these turtle shells have a length less than 85 cm and 10% have a length greater than 103 cm. Find the value of the mean μ and the standard deviation σ .

$$z = \frac{x - \mu}{\sigma}$$

$z = \text{InverseNorm}(0.2, 0, 1) = -0.84$
 $z = \text{InverseNorm}(0.9, 0, 1) = 1.28$

Set up a system of equations to solve for μ and σ : $1.28 = \frac{\sigma}{103 - \mu}$ and $-0.84 = \frac{\sigma}{85 - \mu}$

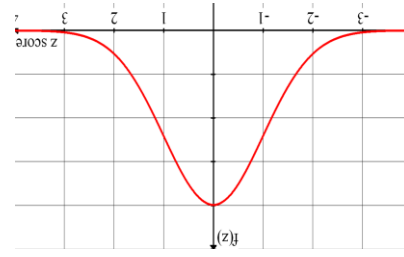
$\mu = 92.1 \text{ cm}$ and $\sigma = 8.5 \text{ cm}$

Z-Scores

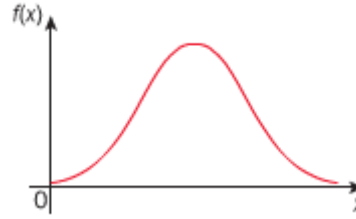
Using the mean and standard deviation of the data, we can standardize the normal distribution by finding the normal deviate, or **z-score**, in each situation. This is done through the formula:

$$z = \frac{x - \mu}{\sigma}$$

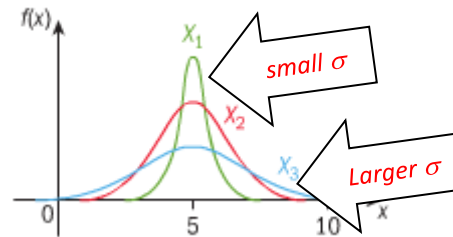
Set the mean to **0** and each 1 unit of the x-axis is **1** standard deviation.



The Normal Curve

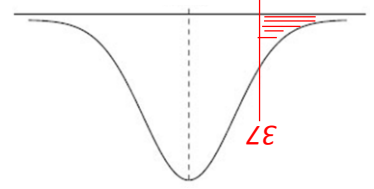


There is no one normal curve; it will **vary** depending on the spread of the data, or **standard deviation**.



Example

The weights of Kemp's ridley (*Leptodochelys kempi*) sea turtles observed off the coast of Florida are normally distributed with a mean of 45 kg and a standard deviation of 4 kg.



A turtle is chosen at random. Find the probability that it weighs less than 37 kg.

Using Empirical Rule: $P(x < 37) = 2.5\%$

Using Calculator: $P(x < 37) = \text{normCDF}(0, 37, 45, 4) = 2.3\%$

Shade the region of the curve that represents this probability.

Properties of the Normal Curve

- The curve is **bell-shaped**.
- It is symmetrical about the **mean**.
- The mean, median, and mode are the **same**.
- The area under the curve represents **100%** of the data.
- The Empirical Rule states **68%** of the data lies within one, **95%** within two, and **99.7%** within three standard deviations from the mean.